

Ecom-Icomp Experts Address Series Feb 27, 2008

Bebo White bebo@slac.stanford.edu

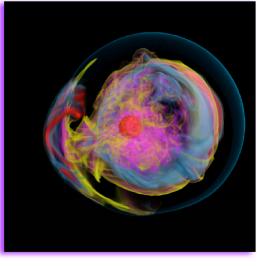
"The first great scientific breakthrough of the 21st century – the decoding of the human genome announced in February 2001 – was a triumph of large-scale computational science. When the Department of Energy (DOE) and the National Institutes of Health (NIH) launched the Human Genome Project in 1990, the most powerful computers were 100,000 times slower than today's high-end machines; private citizens using networks could send data at only 9600 baud; and many geneticists performed their calculations by hand....it was expected to take decades."

---Report to the President, June 2005, "Computational Science: Ensuring America's Competitiveness"

This validates an additional way of "doing science"

# A New Way of Discovery

#### Discovery of the SASI (Standing Accretion Shock Instability)



Blondin & Mezzacappa Nature 445, 58-60 (4 January 2007)

- Wholly computational discovery
- Instability serves to move the shock outward explosion?
- Provides 'natural' explanation for neutron star spin up

NATIONAL CENTER

#### How To "Do Science"

#### The four methods of "doing modern science"

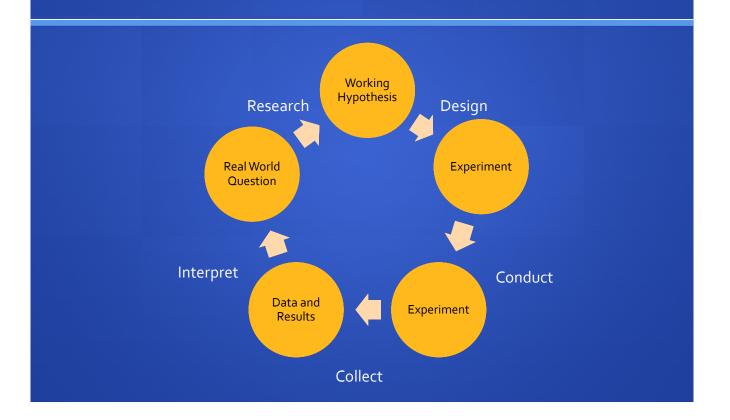








### Scientific Method Process (1/2)



### Scientific Method Process (2/2)

- First described ~400 years ago
- Is not constant evolves as a result of technology
  - Peer review is a result of print
  - Repeatability of experiments is a result of peer review and collaboration (societies, not just letters)
  - Statistical sampling is due to advancements in mathematics
  - Etc.
- The impact of computing is only now being realized

"The underlying physical laws necessary for the mathematical theory of a large part of physics and the whole of chemistry are thus completely known, and the difficulty is only that the exact application of these laws leads to equations much too complicated to be solvable."

--Paul Dirac, Royal Academy, London, 1929

"It is nice to know the computer understands the problem, but I would like to understand it too."

--Eugene Wigner (when confronted with the computer generated results of a quantum mechanics calculation)

#### What is Computational Science? (1/5)

- Computational science is the integration of computing technology into scientific research
- It is the application of computer simulation and other computational methods to the solution of scientific problems and the understanding of scientific phenomenon
- Computing becomes a "full partner" in scientific discovery
- It is not to be confused with computer science which is the study of topics related to computers and information processing

#### Visualization of Computational Science Definition

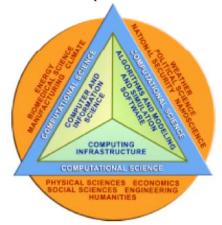


Figure 1

It takes scientific contributions across many disciplines to successfully fit software, systems, networks, and other IT components together to perform computational tasks. And it takes teams of skilled personnel representing those

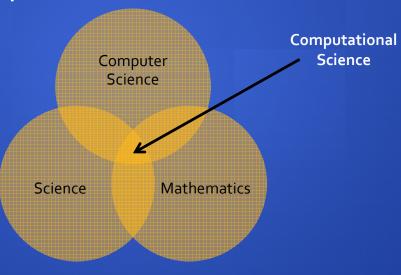
disciplines to manage computing system capabilities and apply them to complicated real-world challenges, much as it takes a medical team with many skills – not just a surgeon with a scalpel – to perform a complex surgical procedure. Indeed, the PITAC believes that the multidisciplinary

The multidisciplinary teams required to address computational science challenges represent what will be the most common mode of 21st century science and engineering R&D.

teams required to address computational science challenges represent what will be the most common mode of science and engineering discovery throughout the 21st century.

#### What is Computational Science? (3/5)

Computational science seeks to gain an understanding of scientific processes through the use of mathematical methods on computers



#### What is Computational Science? (4/5)

#### Used to:

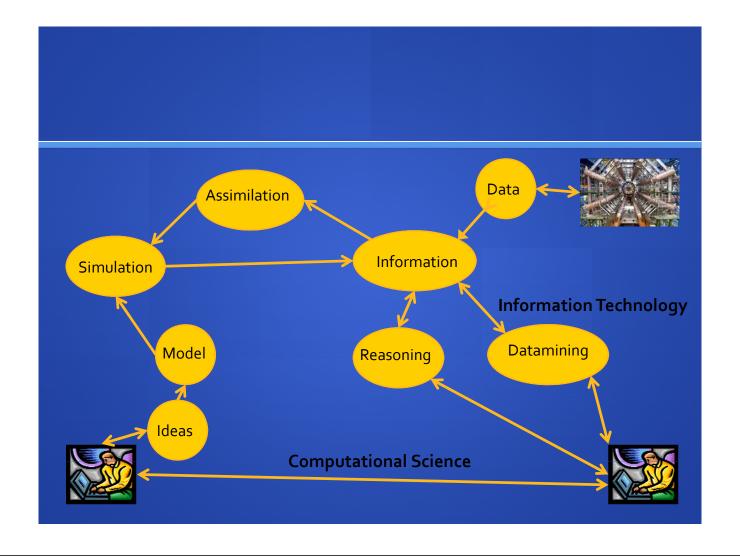
- Perform experiments that might be too dangerous to perform in a lab
- Perform experiments that happen too quickly or too slowly
- Perform experiments that might be too expensive
- Perform experiments that are only solvable using computational approaches
- Visualize phenomenon in the past, present, or future
- Perform "what-if" experiments
- Data mine through huge datasets
- Etc., etc.

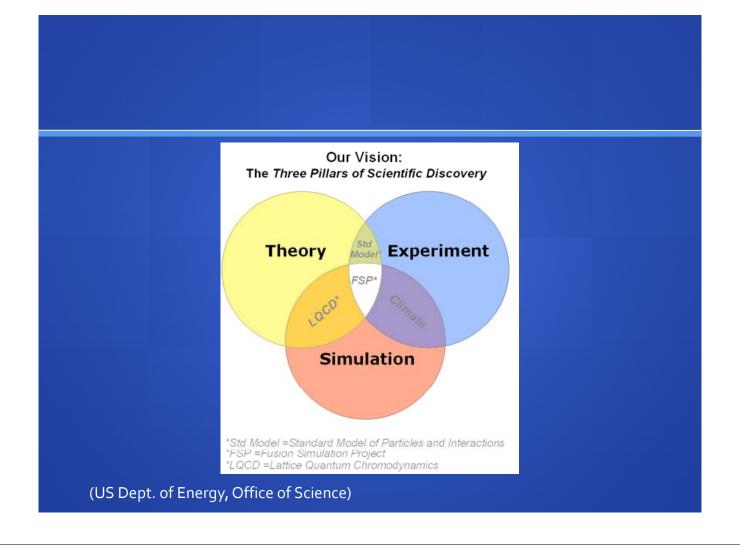
#### What is Computational Science? (5/5)

"Computational Science was built on the vision that computers would represent a virtual laboratory where one could explore new concepts from simulations and comparison of these with experimental data."

---Geoffrey Fox, Indiana University

Analyze - Predict

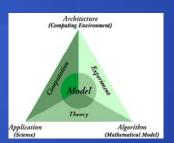




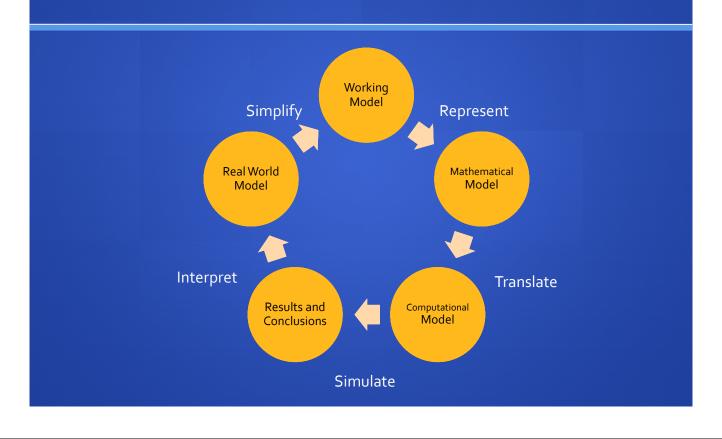
# Computational Science Investigations

### A Computational science investigation should include

- An application a scientific problem of interest and the components of that problem that we wish to study and/or include.
- Algorithm\_- the numerical/mathematical representation of that problem, including any numerical methods or recipes used to solve the algorithm.
- Architecture a computing platform and software tool(s) used to compute a solution set for the algorithm.



#### **Computational Science Process**



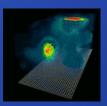
## **The Modeling Process**

- <u>Modeling</u> is the application of methods to analyze complex realworld problems in order to make predictions about what might happen with various actions
- A system exhibits <u>probabilistic</u> or <u>stochastic behavior</u> if an element of chance exists. Otherwise, it exhibits <u>deterministic</u> <u>behavior</u>. A <u>probabilistic</u> or <u>stochastic model</u> exhibits random effects, while a <u>deterministic model</u> does not.
- A <u>static model</u> does not consider time, while a <u>dynamic model</u> changes with time.
- In a <u>continuous model</u>, time changes continuously, while in a <u>discrete model</u> time changes in incremental steps.

(Ref: Shiflet & Shiflet)

# Major Approaches to Computational Science Problems

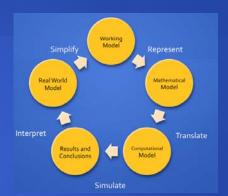
- <u>System dynamics models</u> provide global views of major systems that change with time (e.g., equation-based physics problems)
- <u>Cellular automaton simulations (finite element)</u> provide local views of individuals affecting individuals. The world under consideration consists of a rectangular grid of cells, and each cell has a state that can change with time according to rules (e.g., visualization of lattice gauge QCD)



#### **Real World Problem**

#### Identify Real-World Problem:

- Perform background research, workable problem
- Conduct investigations (Labs)
- Select computational tool
- Understand current activity and predict future behavior



#### **Working Model**

Simplify → \_Working Model:

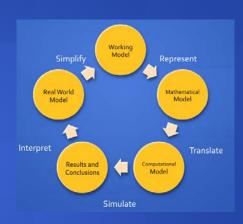
Identify and select factors to

describe important aspects of

Real World Problem; determine

those factors that can be neglected.

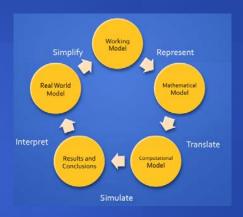
- State simplifying assumptions
- Determine governing principles, physical laws
- Identify model variables and inter-relationships



#### **Mathematical Model**

Represent → Mathematical Model: Express the Working Model in

mathematical terms; write down
mathematical equations or an algorithm
whose solution describes the Working Model.

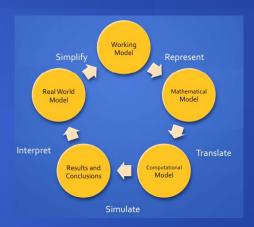


In general, the success of a mathematical model depends on how easy it is to use and how accurately it predicts.

#### **Computational Model**

#### Translate → Computational Model:

- Change *Mathematical Model* into a for computational solution.
- Computational models include tool-specifics.



#### **Results/Conclusions**

Simulate → Results/Conclusions:
Run "Computational Model" to obtain
Results; draw Conclusions.

- Verify your computer program;
   use check cases; explore ranges of validity.
- Graphs, charts, and other visualization tools are useful in summarizing results and drawing conclusions.

#### **Real World Problem**

**Interpret** Conclusions:

Compare with Real World Problem behavior.

physical reality or experimental data, reexamine the Working Model (relax assumptions) and repeat modeling steps.

 Often, the modeling process proceeds through several "cycles" until model is "acceptable"



#### **Example: Projectile Motion**

Determine the motion of a projectile starting from a height H, above the ground with initial velocity V.

### Working Model (1/2)

- Governing principles: d = v\*t and v = a\*t
- Simplifying assumptions:
  - Gravity is the only force acting on the body
  - Flat earth
  - No drag (air resistance)
  - Model variables are H,V, g; t, s, and v

#### Working Model (2/2)

Form a discrete-in-time model to determine the position and velocity of the projectile above the ground at equally spaced times,  $t_0$ ,  $t_1$ ,  $t_2$ , ...,  $t_n$ ; e.g.  $t_0 = 0$  sec,  $t_1 = 1$  sec;  $t_2 = 2$  sec, etc.



#### **Mathematical Model**

Given an initial time,  $t_o$ , an initial height, H, and an initial velocity, V, generate the time history of heights,  $s_n$ , and velocities, v, by the formulas

$$S_0 = H, v_0 = V$$

$$\Delta S_n = v_{n-1} \Delta t, \ S_n = S_{n-1} + \Delta S_n$$

$$\Delta v_n = -g \Delta t, \ v_n = v_{n-1} + \Delta v_n$$

$$n = 1, 2, \cdots$$

### **Computational Model**

#### Pseudo-Code

#### Input

 $t_o$ , initial time; V, initial velocity; H, initial height g, acceleration due to gravity;  $\Delta t$ , time step;  $i_{max}$ , maximum number of steps

#### **Output**

t<sub>i</sub>, t-value at time step i s<sub>i</sub>, height at time t<sub>i</sub> v<sub>i</sub>, velocity at time t<sub>i</sub>

#### **Example: Projectile Motion**

#### <u>Initialize</u>

```
set t_i = t_o = o; v_i = v_o = V; s_i = s_o = H
print t_i, s_i, v_i
```

#### Time stepping: i = 1, $i_{max}$

set 
$$t_i = t_i + \Delta t$$

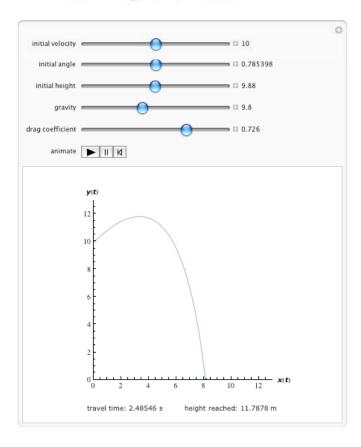
$$set s_i = s_i + v_i * \Delta t$$

set 
$$v_i = v_i - g * \Delta t$$

if 
$$(s_i \le 0)$$
, quit

Wolfram \* Demonstrations Project

#### **Animated Projectile Motion**



#### Interpretation

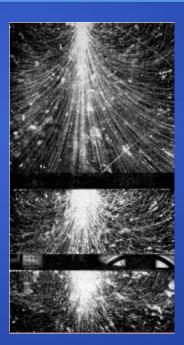
- To create a more more realistic model of a moving projectile, some of the simplifying assumptions could be dropped; e.g., incorporate drag - depends on shape of the projectile, is proportional to velocity
- Improve discrete model:
  - Approximate velocities in the midpoint of time intervals instead of the beginning.
  - Reduce the size of Δt.

# Most Scientific Computing Problems are More Complex Than Moving Projectiles

**Scientific Simulation** 

# Example – Electron-Gamma Showers (EGS)

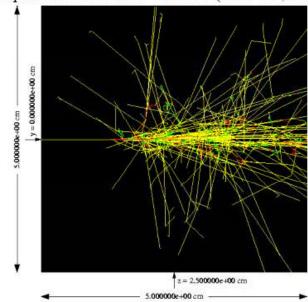
- To simulate the interaction of particle beams of varying energies on fixed targets of various materials and geometries
- To study the resulting particle showers
- Simulations based upon known laws of physics and observed interactions (cross sections) between particles
- Allows "what-ifs" not possible or feasible in the laboratory





#### 1 GeV Photon Shower

1 GeV photon shower in 10 r.l. of Pb (Ecut=0.1, Pcut=0.01 Mev)



# **EGS Applications**

- Materials physics
- Radiation/health physics
- Radiation medicine
- Education
- Etc.

# Finite Element and Lattice Methods

#### Finite Element Method (FEM)

- Many problems in engineering and applied science are governed by differential or integral equations
- The solutions to these equations would provide an exact, closed-form solution to the particular problem being studied
- However, complexities in the geometry, properties and in the boundary conditions that are seen in most real-world problems usually means that an exact solution cannot be obtained or obtained in a reasonable amount of time

#### Finite Element Method (2/2)

- In the FEM, a complex region defining a continuum is discretized into simple geometric shapes called *elements*
- The properties and the governing relationships are assumed over these elements and expressed mathematically in terms of unknown values at specific points in the elements called *nodes*
- An assembly process is used to link the individual elements to the given system. When the effects of loads and boundary conditions are considered, a set of linear or nonlinear algebraic equations is usually obtained
- Solution of these equations gives the *approximate* behavior of the continuum or system

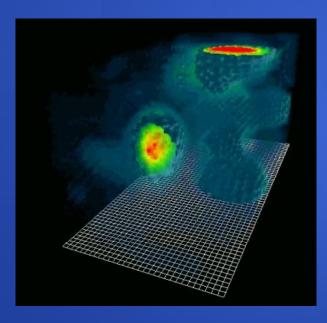
#### Example – Lattice QCD Simulation (1/3)

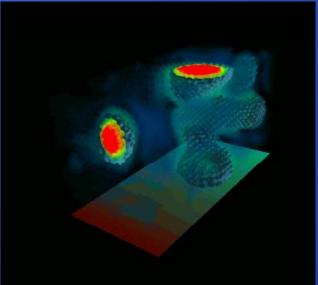
- In quantum theories such as QCD, particles are represented by fields
- To simulate the quark and gluon activities inside matter on a computer, physicists calculate the evolution of the fields on a fourdimensional lattice representing space and time
- A typical lattice simulation that approximates a volume containing a proton might use a grid of 24x24x24 points in space evaluated over a sequence of 48 points in time
- The values at the intersections of the lattice approximate the local strength of quark fields
- The links between the points simulate the rubber bands—the strength
  of the gluon fields that carry energy and other properties of the strong
  force through space and time, manipulating the quark fields.

#### Example – Lattice QCD Simulation (2/3)

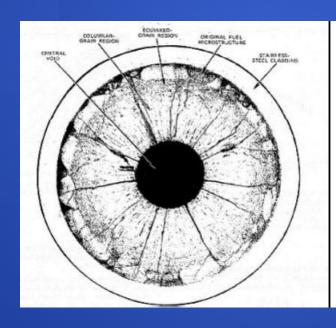
- At each step in time, the computer recalculates the field strengths at each point and link in space
- The algorithm for a single point takes into account the changing fields at the eight nearest-neighbor points, representing the exchange of gluons in three directions of space-up and down; left and right; front and back-and the change of the fields over time-past and future.

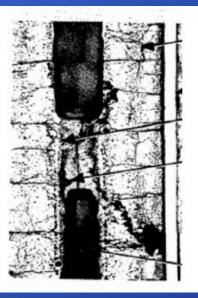
# Example – Lattice QCD Simulation (3/3)





# **Nuclear Fuel Rod Degradation**





# Advanced Test Reactor Simulation at INL (Idaho National Laboratory)



#### Simulation vs. CGI?

http://www.youtube.com/watch?v= FIKonHQF8Y

# Topics in Computational Science and Engineering

- High Performance Computing
- Data Mining
- Simulation
- Scientific Visualization
- Programming (Traditional and Symbolic Manipulation Tools)
- Collaboration systems/E-Science
- Analysis Packages
- Display and text processing systems

### **Data Mining**

### **Data Mining**

- Modern science is driven by data analysis like never before.
   We have an ability to collect and process data that is increasing exponentially!
- "...the analysis of (often large) observational data sets to find unsuspected relationships and to summarize the data in novel ways that are both understandable and useful to the data owner."
- The extraction of useful patterns from data sources, e.g., databases, texts, web, image.

- Sequential pattern mining:
  - A sequential rule:  $A \rightarrow B$ , says that event A will be immediately followed by event B with a certain confidence
- Deviation/anomaly/exception detection: discovering the most significant changes in data
- Data visualization: using graphical methods to show patterns in data
- High performance computing
- Bioinformatics

#### Why Data Mining

- Rapid computerization produces huge amounts of data
- How to make best use of data?
- A growing realization: knowledge discovered from data can be used for competitive advantage and to increase intelligence

### **Purposes of Data Mining**

- Locating phenomenon from spatially, temporally, or logically related factors, each of which is defined at different levels of abstraction
- Content based searching and browsing
- Feature extraction
- Reduction in data volume
- Scientific analysis
- Searching for anomalies

#### **Data Mining Fields**

Data mining is an emerging multi-disciplinary field:

**Statistics** 

**Machine learning** 

**Databases** 

Visualization

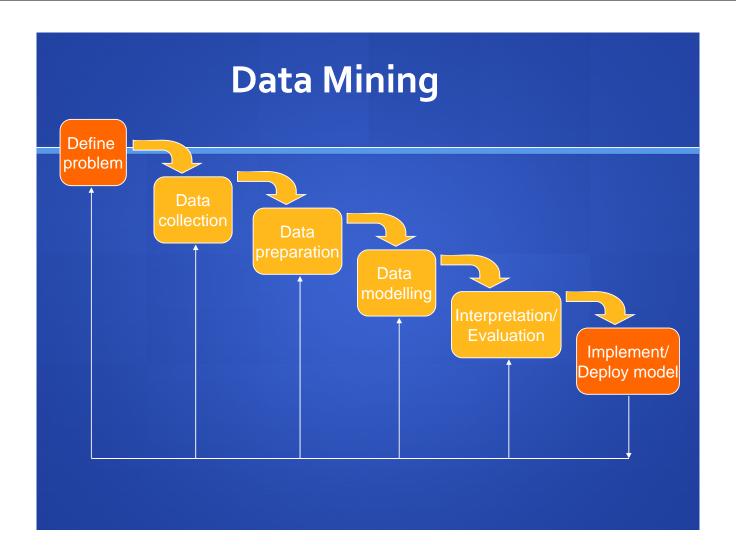
**Data warehousing** 

**High-performance computing** 

...

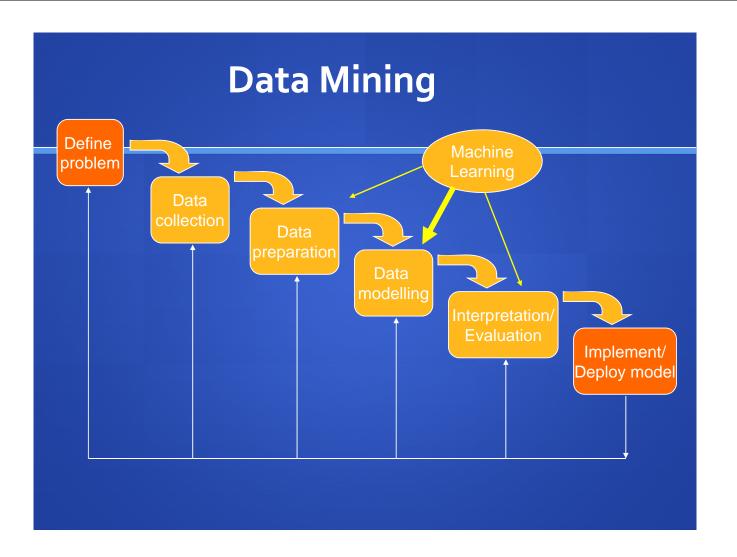
### **Typical Data Mining Tasks**

- Classification:
  - mining patterns that can classify future data into known classes
- Association rule mining:
  - mining any rule of the form  $X \rightarrow Y$ , where X and Y are sets of data items
- Clustering:
  - identifying a set of similar groups in the data



#### **Machine Learning**

- "...the study of computer algorithms capable of learning to improve their performance on a task on the basis of their own experience."
  - Often this is "learning from data".
- A sub-discipline of artificial intelligence, with large overlaps into statistics, pattern recognition, visualization, robotics, control, ...



#### Patterns (1/2)

- Patterns are the relationships and summaries derived through a data mining exercise
- Patterns must be:
  - valid
  - novel
  - potentially useful
  - understandable

#### Patterns (2/2)

- Patterns are used for
  - prediction or classification
  - describing the existing data
  - segmenting the data (e.g., the market)
  - profiling the data (e.g., your customers)
  - Detection (e.g., intrusion, fault, anomaly)

#### **Data(1/2)**

- Data mining typically deals with data that have already been collected for some purpose other than data mining
- Data miners usually have no influence on data collection strategies
- Large bodies of data cause new problems: representation, storage, retrieval, analysis, ...

#### Data (2/2)

- Even with a very large data set, we are usually faced with just a sample from the population.
- Data exist in many types (continuous, nominal) and forms (credit card usage records, supermarket transactions, government statistics, text, images, medical records, human genome databases, molecular databases).

# Data Modelling and the Scientific Method

- Data modelling plays an important role at several stages in the scientific process:
  - Observe and explore interesting phenomena
  - Generate hypotheses
  - 3. Formulate model to explain phenomena
  - 4. Test predictions made by the theory
  - Modify theory and repeat (at 2 or 3)
- The explosion of data suggests that we need to (partially) automate numerous aspects of the scientific method

### **Pattern Recognition**

### **Pattern Recognition**

- Pattern recognition is a research area in which pattern in data are found, measured, and used to recognize, classify and discover objects
- This is a catchall phrase that includes:
  - Classification
  - Clustering
  - Data mining
  - etc

### Pattern Recognition Approaches

- Statistical Pattern Recognition
  - The data is reduced to vectors of real numbers that measure objects features. Statistical modeling is then used for recognition, classification, etc
- Structural Pattern Recognition
  - The data is converted to a discrete and structured form such as trees, graphs, grammars, etc. Techniques related to computer science subjects such as graph matching and parsing are used

#### **Scientific Visualization**

#### The Challenge

- Transform the data into information (understanding, insight) thus making it useful to people.
- Support specific tasks
- Improve performance as compared to existing mechanisms

#### Information Visualization

- Provide tools that present data in a way to help people understand and gain insight from it
- Cliches
  - "Seeing is believing"
  - "A picture is worth a thousand words"

"The use of computer-supported, interactive, visual representations of abstract data to amplify cognition."

#### **Main Idea**

- Visuals help us think
  - Provide a frame of reference, a temporary storage area
- External cognition
  - Role of external world in thinking and reason
  - Multiplication exercise

#### Information Visualization

- What is "information"?
  - Items, entities, things which do not have a direct physical correspondence
  - Examples: baseball statistics, stock trends, connections between criminals, car attributes...
- Scientific Visualization
  - Primarily relates to and represents something physical or geometric
  - Examples
    - Air flow over a wing
    - Stresses on a girder
    - Weather over Pennsylvania

#### **Key Attributes**

- Scale
  - Challenge often arises when data sets become very large
- Interactivity
  - Want to show multiple different perspectives on the data
- Tasks
  - Want to support specific tasks not just to create a cool demo
  - Support discovery, decision making, explanation

#### **Visualization Success Stories**

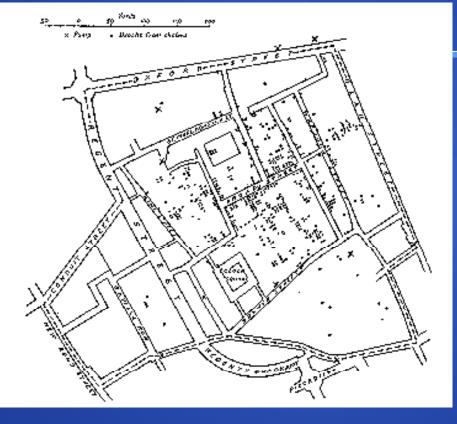
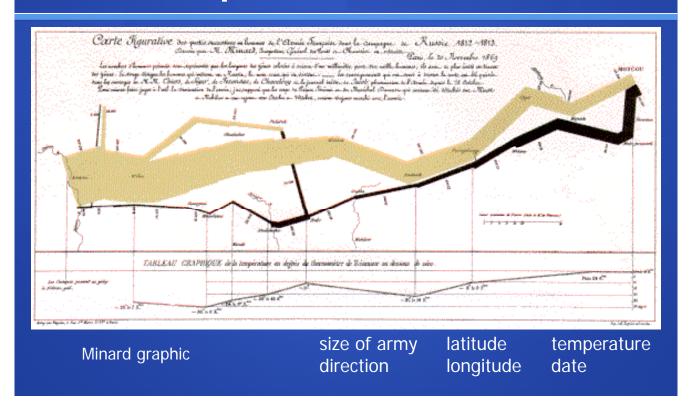


Illustration of John Snow's deduction that a cholera epidemic was caused by a bad water pump, circa 1854.

Dots indicate location of deaths.

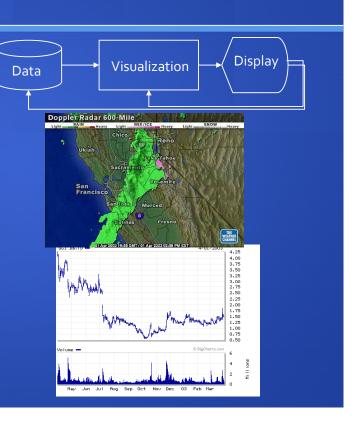
From Visual Explanations by Edward Tufte, Graphics Press, 1997

### Napoleon's March



#### What is Scientific Visualization?

- It is a transformation of abstract data into readily-comprehensible images
- It relies on human cognitive processes



# Geometric and Visual Computing Areas

- Computer Aided Geometric Design (CAGD): Curves/surfaces
- Solid Modeling: Representations and Algorithms for solids
- Computational Geometry: Provably efficient algorithms
- Computer-Aided Design (CAD): Automation of Shape Design
- Computer-Aided Manufacturing (CAM): NC Machining
- Finite Element Meshing (FEM): Construction and simulation

# New Topics in Computational Science and Engineering

- "Collaboratories" and scientific workspaces of the future
- Scientific research in virtual worlds
- Exascale Science
- Web Science

# Programming and Mathematical Solvers

# Popular Symbolic/Mathematical Software Packages (1/2)

#### Mathematica

- Advantages premier all-purpose mathematical software package; It integrates swift and accurate symbolic and numerical calculation, allpurpose graphics, and a powerful programming language
- Disadvantages Steep learning curve, expensive; premier allpurpose mathematical software package. It integrates swift and accurate symbolic and numerical calculation, all-purpose graphics, and a powerful programming language

#### Matlab

- Advantages combines efficient computation, visualization and programming for linear-algebraic technical work and other mathematical areas
- Disadvantages Not for analytical/symbolic math

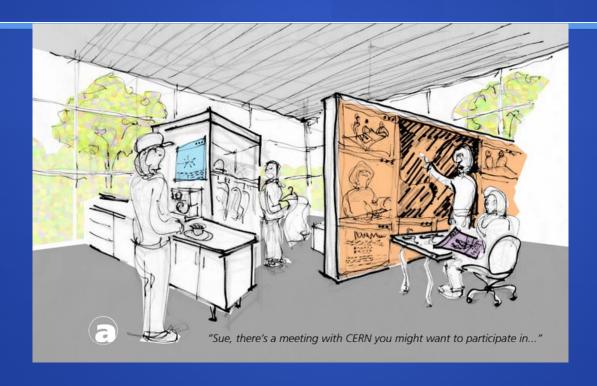
# Popular Symbolic/Mathematical Software Packages (2/2)

#### Maple

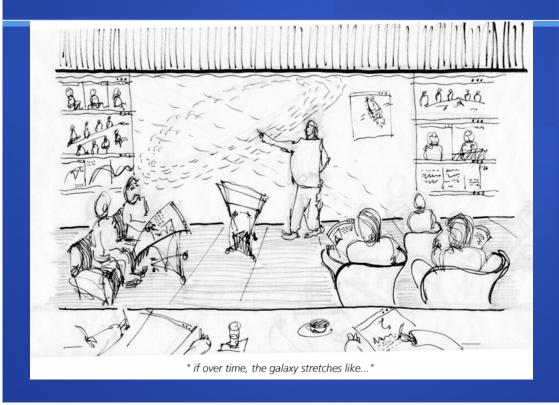
- Advantages powerful analytical and mathematical software which does the same sorts of things that Mathematica does, with similar high quality; programming language is procedural -- like C or Fortran or Basic -- although it has a few functional programming constructs.
- Disadvantages Worksheet interface/typesetting not as developed as Mathematica's, but it is less expensive
- IDL (Interactive Data Language)
  - Advantages excels at processing real-world data, especially graphics, and has a reasonably simple syntax, especially for those familiar with Fortran or C; makes it as easy as possible to read in data from files of numerous scientific data formats
  - Disadvantages Does not do symbolic math

# Scientific Workspace of the Future (SWOF)

### **Ad Hoc Collaboration**



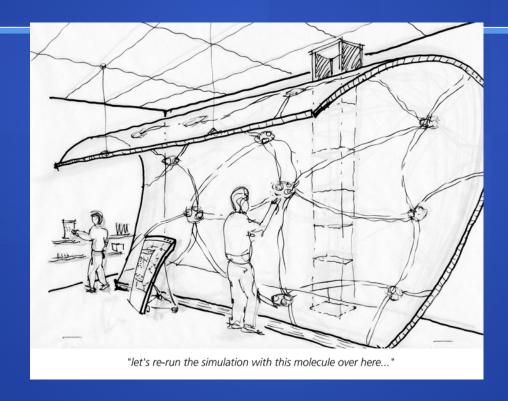
### **Distance Learning**



# **Distributed Exploratory Analysis**



### **Interactive Scientific Computing**



REVIEWS

#### The Scientific Research Potential of Virtual Worlds

William Sims Bainbride

Other virtual worlds, electronic revisionments where people can work and interest in a somewhall medicist manner, how great potential as sifts for research in the scale), behavioral, and economic sciences, as well as in human-centered componer science. This article some Second Life and Wind of Bisscrat, as how very efficience excepts of current virtual worlds that fore-badow force developments, smokeling a monther of ensearch methodologies that scientific are now for economic such section of the science of the except of the science of the control of economic such section of the science of the

whose solies worldike onivoreness have made possible rew kinds of resconds in the social and balancial sciences, such estimated the social and balancial sciences, such estimated the solies of computer and for induction arous all the science (1,2). We can use the term's visit would be absorbed to all control and the science (1,2) which is the science of the science

and by seccify, the marks via a presented computer tempting special softwards and contracts to see on more errors that gases information back and feath between teams on the fauncies. But an information back and softwards are supported to the fauncies and the second section of the s

In terms of scientific research methodologics, one can do interviews and oftwographic research in both environments, but other methods would work better in one than the other. St. in especially well designed to mount formal experiments in social psychology or cognitive

Ownton of Information and Intelligent Systems, National Science Foundation, 4201 Wilson Boolevard, Arlington, VE 22230, USA. earth methodologies that scientists are now validonal ethnography, and quantitative analysis science, because the researcher can construct a facility comparable to a real-world laboratory and recruit mearch subjects. Wolf may be better for nonintrusive statistical methodologies examining social networks and economic systems, because in strately generates a vast frow or directs but in strately generates a vast frow or directs but

The present montants are stated than The present memer transles at major historical transition. Video games and computer games are in the process of evolving into sexterding much richer, numely virtual worlds, at the same time that electronic games are suprassing the restion picture industry in dollar terms and beginning to cut into television. Already, many families forgounkfully IV dammes to quest together in Wolf.

sication are menging in what Americans cell resistance comparing. The currum generation of visible experiments of the currum generation of visible to the comparing the currum generation of visible to the Niteration William of the Niteration Stoth for Niteration William Stoth for Niteration William Stoth for the Niteration Stoth for the comparing are proliferation. However, the content are exploring the methods needed to create an exploring the methods needed to create an exploring the methods needed to create an over LASP, (three-action reflectpring general) that have pulsers act in the real world while simultaneously interacting over the literate visible simultaneously interacting over the literate visible simultaneously structured in the simultane

states, in exceeding planted in entanties are discovered produced by the care for example, a Web see called Revisional that was merely shoot Web records yield for inflame of the most planted by the called Revisional that was merely shoot Web records yield for inflame of the most planted by the called the ca

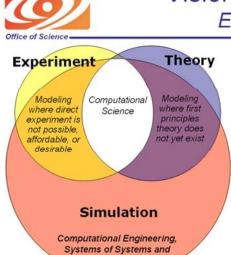


Fig. 1. The Stormwind Auction House in Wolff. The three figures searing wests and standing on platforms are the computer generated auctioners, whereas the dozen other figures are characters belonging to real brunnal being participating in auctions involving a thousand or more people. The one warring is the control in the avutar of a scientist who is studying this virtual world and the computer-suisted systems it provides to facilitate social interaction and encountie exchange.

Online virtual worlds have great potential as sites for research in the social, behavioral, and economic sciences, as well as in human-centered computer science. A number of research methodologies are being explored, including formal experimentation, observational ethnography, and quantitative analysis of economic markets or social networks.

472

27 JULY 2007 VOL 317 SCIENCE www.sciencemag.org



Virtual Prototyping

Vision for Future Exascale

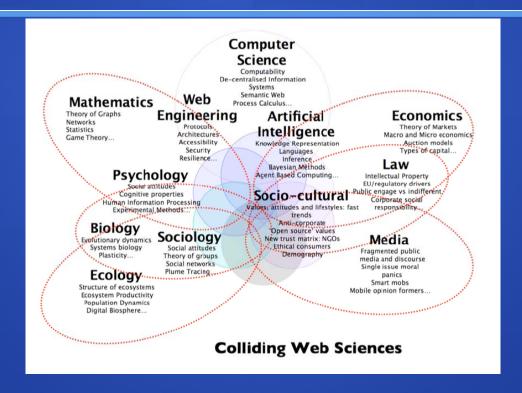
Moving Simulation toward broad acceptance throughout scientific research and industry - greatly informing theory and experiment and even replacing some experiments

Lower uncertainty in simulations to support decisions

Bigger, more accurate models – positioning the United States to sustain its computational leadership and economic competitiveness

9

#### **Web Science**



# What is a Computational Scientist?



Campus Information Technology Committees • The University of Georgia

#### Computational Scientist Degree: Learning Outcomes and Objectives

July 21, 1995

Students completing this program will:

- · Be prepared to join and contribute to interdisciplinary teams in scientific research or industry.
- Have a firm understanding of the physical theory and computational strategies used in the student's major discipline. This includes the ability to select the most appropriate algorithm for the problem.
- · Understand the computational methods used in the industry standard software packages in the student's major discipline.
- . Have a general knowledge of the computational methods used in other areas and their potential application to the student's major discipline.
- · Have a solid foundation in numerical methods and a general understanding of statistical data analysis.
- · Understand computer architectures used in modern scientific computation.
- Be familiar with currently used programming languages for scientific computing (C, FORTRAN 90 and FORTRAN 77) including optimization techniques
- · Have an in-depth understanding of parallel algorithm development and other methods and tools required for high performance computing.
- Be able to apply the tools of visualization to the analysis of scientific data and produce images/animations that extract the essential information and display it so the relevant content is clear.
- Have demonstarated ability in creating useful tools for computational scientific research. The tools needed are those that are powerful and flexible enough to solve a variety of real problems, safe to run and optimized enough to handle large problems.

#### **Phantom Works**

#### **Engineering and Information Technology**

#### Mathematics and Engineering Analysis

M&CT's Mathematics and Engineering Analysis unit is Boeing's central math resource -- about 100 mathematicians and scientists with extensive experience in industrial R&D and problem solving. The organization's experts are skilled in applied statistics, computational science, computational linear algebra and differential equations, geometry and optimization, mathematical modeling, operations research, and modeling and simulations technology. They work with engineers and other technologists on the design and manufacturing of commercial airplanes and military and space systems. They also conduct applied R&D and do consulting and software development for non-Boeing customers.

#### Applied Statistics

The Applied Statistics group is devoted to a combination of R&D and consulting in support of aerospace industry needs. Their work ranges through most standard areas of industrial statistics: survey design and analysis, time series and forecasting, probability and stochastic models, statistical quality control, Design of Experiments (DOE), and reliability.

The aerospace industry, rich in diverse and complex problems, has led us to other areas including image processing, spatial statistics, industrial epidemiology, data mining, design and analysis of computer experiments, Bayesian information retrieval, financial modeling, stochastic optimization, and statistical tolerancing.

#### Computational Science

The Computational Science group provides software and support to Boeing engineers and mathematicians engaged in solving the mathematical problems that arise while using computers to design complex structures and aircraft and simulate airflow.

The group's areas of expertise include:

- Application of parallel computing techniques to mathematical computation
- Web-enabled delivery and analysis tools
- Advanced engineering computing techniques
- ▶ C, C++, Fortran, Java, and Visual Basic programming languages
- Mathematical software

#### Thank You

**Questions, Comments?** 

bebo@slac.stanford.edu